

# Package ‘mosum’

March 17, 2021

**Title** Moving Sum Based Procedures for Changes in the Mean

**Version** 1.2.5

**Date** 2021-03-17

**Description** Implementations of MOSUM-based statistical procedures and algorithms for detecting multiple changes in the mean. This comprises the MOSUM procedure for estimating multiple mean changes from Eichinger and Kirch (2018) <doi:10.3150/16-BEJ887> and the multi-scale algorithmic extensions from Cho and Kirch (2019) <arXiv:1910.12486>. See Meier, Kirch and Cho (2021) <doi:10.18637/jss.v097.i08> which accompanies the R package.

**Depends** R (>= 3.1.2)

**License** GPL (>= 3)

**LazyData** true

**Imports** RColorBrewer, plot3D, Rcpp (>= 0.12.5)

**LinkingTo** Rcpp

**Maintainer** Haeran Cho <haeran.cho@bristol.ac.uk>

**RoxygenNote** 7.1.1

**Encoding** UTF-8

**NeedsCompilation** yes

**Author** Alexander Meier [aut],  
Haeran Cho [aut, cre],  
Claudia Kirch [aut]

**Repository** CRAN

**Date/Publication** 2021-03-17 16:20:06 UTC

## R topics documented:

bandwidths.default . . . . .	2
confint.mosum.cpts . . . . .	3
confint.multiscale.cpts . . . . .	4
mosum . . . . .	5
mosum.criticalValue . . . . .	7

multiscale.bottomUp . . . . .	8
multiscale.localPrune . . . . .	10
persp3D.multiscaleMosum . . . . .	12
plot.mosum.cpts . . . . .	14
plot.multiscale.cpts . . . . .	15
print.mosum.cpts . . . . .	16
print.multiscale.cpts . . . . .	17
summary.mosum.cpts . . . . .	18
summary.multiscale.cpts . . . . .	18
testData . . . . .	19

<b>Index</b>	<b>21</b>
--------------	-----------

---

bandwidths.default	<i>Default choice for the set of multiple bandwidths</i>
--------------------	--

---

## Description

Create bandwidths according to a default function of the sample size

## Usage

```
bandwidths.default(n, d.min = 10, G.min = 10, G.max = min(n/2, n^(2/3)))
```

## Arguments

n	integer representing the sample size
d.min	integer for the minimal mutual distance of change-points that can be expected
G.min	integer for the minimal allowed bandwidth
G.max	integer for the maximal allowed bandwidth

## Details

Returns an integer vector of bandwidths  $(G_1, \dots, G_m)$ , with  $G_0 = G_1 = \max(G_{\min}, 2/3 \cdot d_{\min})$ ,  $G_{j+1} = G_{j-1} + G_j$  (for  $j = 1, \dots, m-1$ ) and  $m$  satisfying  $G_m \leq G_{\max}$  while  $G_{m+1} > G_{\max}$ .

## Value

an integer vector of bandwidths

## References

A. Meier, C. Kirch and H. Cho (2021) mosum: A Package for Moving Sums in Change-point Analysis. *Journal of Statistical Software*, Volume 97, Number 8, pp. 1-42. <doi:10.18637/jss.v097.i08>.

H. Cho and C. Kirch (2020) Two-stage data segmentation permitting multiscale change points, heavy tails and dependence. *arXiv preprint arXiv:1910.12486*.

**Examples**

```
bandwidths.default(1000, 10, 10, 200)
```

---

```
confint.mosum.cpts      Confidence intervals for change-points
```

---

**Description**

Generate bootstrap confidence intervals for change-points.

**Usage**

```
## S3 method for class 'mosum.cpts'
confint(object, parm = "cpts", level = 0.05, N_reps = 1000, ...)
```

**Arguments**

object	an object of class mosum.cpts
parm	specification of which parameters are to be given confidence intervals; parm = "cpts" is supported
level	numeric value in (0, 1), such that the 100(1-level)% confidence bootstrap intervals are computed
N_reps	number of bootstrap replications
...	not in use

**Details**

See the referenced literature for further details

**Value**

S3 object of class cpts.ci, containing the following fields:

level, N_reps	input parameters
CI	data frame of five columns, containing the estimated change-points (column cpts), the pointwise confidence intervals (columns pw.left and pw.right) and the uniform confidence intervals (columns unif.left and unif.right) for the corresponding change-points

**References**

A. Meier, C. Kirch and H. Cho (2021) mosum: A Package for Moving Sums in Change-point Analysis. *Journal of Statistical Software*, Volume 97, Number 8, pp. 1-42. <doi:10.18637/jss.v097.i08>.

**Examples**

```
x <- testData(lengths = rep(100, 3), means = c(0, 3, 1), sds = rep(1, 3), seed = 1337)$x
m <- mosum(x, G = 40)
ci <- confint(m, N_reps = 5000)
print(ci$CI)
```

---

confint.multiscale.cpts

*Confidence intervals for change-points*

---

**Description**

Generate bootstrap confidence intervals for change-points.

**Usage**

```
## S3 method for class 'multiscale.cpts'
confint(object, parm = "cpts", level = 0.05, N_reps = 1000, ...)
```

**Arguments**

object	an object of class multiscale.cpts
parm	specification of which parameters are to be given confidence intervals; parm = "cpts" is supported
level	numeric value in (0, 1), such that the 100(1-level)% confidence bootstrap intervals are computed
N_reps	number of bootstrap replications
...	not in use

**Details**

See the referenced literature for further details

**Value**

S3 object of class cpts.ci, containing the following fields:

level, N_reps	input parameters
CI	data frame of five columns, containing the estimated change-points (column cpts), the pointwise confidence intervals (columns pw.left and pw.right) and the uniform confidence intervals (columns unif.left and unif.right) for the corresponding change-points

**References**

A. Meier, C. Kirch and H. Cho (2021) mosum: A Package for Moving Sums in Change-point Analysis. *Journal of Statistical Software*, Volume 97, Number 8, pp. 1-42. <doi:10.18637/jss.v097.i08>.

**Examples**

```
x <- testData(lengths = rep(100, 3), means = c(0, 3, 1), sds = rep(1, 3), seed = 1337)$x
mlp <- multiscale.localPrune(x, G = c(8, 15, 30, 70))
ci <- confint(mlp, N_reps = 5000)
print(ci$CI)
```

mosum

*MOSUM procedure for multiple change-point estimation***Description**

Computes the MOSUM detector, detects (multiple) change-points and estimates their locations.

**Usage**

```
mosum(
  x,
  G,
  G.right = G,
  var.est.method = c("mosum", "mosum.min", "mosum.max", "custom")[1],
  var.custom = NULL,
  boundary.extension = TRUE,
  threshold = c("critical.value", "custom")[1],
  alpha = 0.1,
  threshold.custom = NULL,
  criterion = c("eta", "epsilon")[1],
  eta = 0.4,
  epsilon = 0.2,
  do.confint = FALSE,
  level = 0.05,
  N_reps = 1000
)
```

**Arguments**

<code>x</code>	input data (a numeric vector or an object of classes <code>ts</code> and <code>timeSeries</code> )
<code>G</code>	an integer value for the moving sum bandwidth; <code>G</code> should be less than <code>length(n)/2</code> . Alternatively, a number between 0 and 0.5 describing the moving sum bandwidth relative to <code>length(x)</code> can be given
<code>G.right</code>	if <code>G.right != G</code> , the asymmetric bandwidth ( <code>G, G.right</code> ) will be used; if <code>max(G, G.right)/min(G, G.right) &gt; 4</code> , a warning message is generated
<code>var.est.method</code>	how the variance is estimated; possible values are <ul style="list-style-type: none"> <li>"mosum" both-sided MOSUM variance estimator</li> <li>"mosum.min" minimum of the sample variance estimates from the left and right summation windows</li> </ul>

- "mosum.max" maximum of the sample variance estimates from the left and right summation windows
- "custom" a vector of length(x) is to be parsed by the user; use var . custom in this case to do so

var.custom      a numeric vector (of the same length as x) containing local estimates of the variance or long run variance; use iff var . est . method = "custom"

boundary.extension      a logical value indicating whether the boundary values should be filled-up with CUSUM values

threshold      string indicating which threshold should be used to determine significance. By default, it is chosen from the asymptotic distribution at the given significance level alpha. Alternatively it is possible to parse a user-defined numerical value with threshold . custom

alpha      a numeric value for the significance level with  $0 \leq \alpha \leq 1$ ; use iff threshold = "critical.value"

threshold . custom      a numeric value greater than 0 for the threshold of significance; use iff threshold = "custom"

criterion      string indicating how to determine whether each point k at which MOSUM statistic exceeds the threshold is a change-point; possible values are

- "eta" there is no larger exceeding in an  $\eta * G$  environment of k
- "epsilon" k is the maximum of its local exceeding environment, which has at least size  $\epsilon * G$

eta      a positive numeric value for the minimal mutual distance of changes, relative to moving sum bandwidth (iff criterion = "eta")

epsilon      a numeric value in (0,1] for the minimal size of exceeding environments, relative to moving sum bandwidth (iff criterion = "epsilon")

do.confint      flag indicating whether to compute the confidence intervals for change-points

level      use iff do.confint = TRUE; a numeric value ( $0 \leq \text{level} \leq 1$ ) with which  $100(1-\text{level})\%$  confidence interval is generated

N\_reps      use iff do.confint = TRUE; number of bootstrap replicates to be generated

### Value

S3 object of class mosum.cpts, which contains the following fields:

x	input data
G.left, G.right	left and right summation bandwidths
var.est.method, var.custom, boundary.extension	input parameters
stat	a series of MOSUM statistic values; the first G and last G.right values are NA iff boundary.extension = FALSE
rollsums	a series of MOSUM detector values; equals stat*sqrt(var.estimation)

`var.estimation` the local variance estimated according to `var.est.method`  
`threshold`, `alpha`, `threshold.custom`  
input parameters  
`threshold.value`  
threshold value of the corresponding MOSUM test  
`criterion`, `eta`, `epsilon`  
input parameters  
`cpts`  
a vector containing the estimated change-point locations  
`cpts.info`  
data frame containing information about change-point estimators including de-  
tection bandwidths, asymptotic p-values for the corresponding MOSUM statis-  
tics and (scaled) size of jumps  
`do.confint`  
input parameter  
`ci`  
S3 object of class `cpts.ci` containing confidence intervals for change-points iff  
`do.confint=TRUE`

## References

A. Meier, C. Kirch and H. Cho (2021) mosum: A Package for Moving Sums in Change-point Anal-  
ysis. *Journal of Statistical Software*, Volume 97, Number 8, pp. 1-42. <doi:10.18637/jss.v097.i08>.  
B. Eichinger and C. Kirch (2018) A MOSUM procedure for the estimation of multiple random  
change-points. *Bernoulli*, Volume 24, Number 1, pp. 526-564.

## Examples

```

x <- testData(lengths = rep(100, 3), means = c(0, 5, -2), sds = rep(1, 3), seed = 1234)$x
m <- mosum(x, G = 40)
plot(m)
summary(m)

```

---

mosum.criticalValue    *MOSUM asymptotic critical value*

---

## Description

Computes the asymptotic critical value for the MOSUM test.

## Usage

```
mosum.criticalValue(n, G.left, G.right, alpha)
```

## Arguments

`n`  
an integer value for the length of the input data  
`G.left`, `G.right`  
integer values for the left and right moving sum bandwidth (`G.left`, `G.right`)  
`alpha`  
a numeric value for the significance level with  $0 \leq \alpha \leq 1$

**Value**

a numeric value for the asymptotic critical value for the MOSUM test

**Examples**

```
x <- testData(lengths = rep(100, 3), means = c(0, 5, -2), sds = rep(1, 3), seed = 1234)$x
m <- mosum(x, G = 40)
par(mfrow = c(2, 1))
plot(m$stat, type = "l", xlab = "Time", ylab = "", main = "mosum")
abline(h = mosum.criticalValue(300, 40, 40, .1), col = 4)
abline(v = m$cpts, col = 2)
plot(m, display = "mosum") # identical plot is produced
```

---

multiscale.bottomUp    *Multiscale MOSUM algorithm with bottom-up merging*

---

**Description**

Multiscale MOSUM procedure with symmetric bandwidths combined with bottom-up bandwidth-based merging.

**Usage**

```
multiscale.bottomUp(
  x,
  G = bandwidths.default(length(x), G.min = max(20, ceiling(0.05 * length(x)))),
  threshold = c("critical.value", "custom")[1],
  alpha = 0.1,
  threshold.function = NULL,
  eta = 0.4,
  do.confint = FALSE,
  level = 0.05,
  N_reps = 1000,
  ...
)
```

**Arguments**

x	input data (a numeric vector or an object of classes <code>ts</code> and <code>timeSeries</code> )
G	a vector of (symmetric) bandwidths, given as either integers less than $\text{length}(x)/2$ , or numbers between 0 and 0.5 describing the moving sum bandwidths relative to $\text{length}(x)$ . If the smallest bandwidth is smaller than $\min(20, 0.05 \cdot \text{length}(x))$ (0.05 if relative bandwidths are given) and <code>threshold = "critical.value"</code> , it generates a warning message
threshold	string indicating which threshold should be used to determine significance. By default, it is chosen from the asymptotic distribution at the given significance level <code>alpha</code> . Alternatively, it is possible to parse a user-defined function with <code>threshold.function</code>



alpha	a numeric value for the significance level with $0 \leq \alpha \leq 1$ ; use iff threshold = "critical.value"
threshold.function	function object of form <code>function(G, length(x), alpha)</code> , to compute a threshold of significance for different bandwidths G; use iff threshold = "custom"
eta	see <a href="#">mosum</a>
do.confint	flag indicating whether to compute the confidence intervals for change-points
level	use iff do.confint = TRUE; a numeric value ( $0 \leq \text{level} \leq 1$ ) with which $100(1-\text{level})\%$ confidence interval is generated
N_reps	use iff do.confint = TRUE; number of bootstrap replicates to be generated
...	further arguments to be passed to the <a href="#">mosum</a> calls

### Details

See Algorithm 1 in the first referenced paper for a comprehensive description of the procedure and further details.

### Value

S3 object of class `multiscale.cpts`, which contains the following fields:

x	input data
cpts	estimated change-points
cpts.info	data frame containing information about estimated change-points
pooled.cpts	set of change-point candidates that have been considered by the algorithm
G	bandwidths
threshold, alpha, threshold.function	input parameters
eta	input parameters
do.confint	input parameter
ci	object of class <code>cpts.ci</code> containing confidence intervals for change-points iff do.confint = TRUE

### References

- A. Meier, C. Kirch and H. Cho (2021) `mosum`: A Package for Moving Sums in Change-point Analysis. *Journal of Statistical Software*, Volume 97, Number 8, pp. 1-42. <doi:10.18637/jss.v097.i08>.
- M. Messer et al. (2014) A multiple filter test for the detection of rate changes in renewal processes with varying variance. *The Annals of Applied Statistics*, Volume 8, Number 4, pp. 2027-2067.

**Examples**

```
x1 <- testData(lengths = c(100, 200, 300, 300),
means = c(0, 1, 2, 2.7), sds = rep(1, 4), seed = 123)$x
mbu1 <- multiscale.bottomUp(x1)
plot(mbu1)
summary(mbu1)

x2 <- testData(model = "mix", seed = 1234)$x
threshold.custom <- function(G, n, alpha) {
mosum.criticalValue(n, G, G, alpha) * log(n/G)^0.1
}
mbu2 <- multiscale.bottomUp(x2, G = 10:40, threshold = "custom",
threshold.function = threshold.custom)
plot(mbu2)
summary(mbu2)
```

---

multiscale.localPrune *Multiscale MOSUM algorithm with localised pruning*

---

**Description**

Multiscale MOSUM procedure with (possibly) assymmetric bandwidths and localised pruning based on Schwarz criterion.

**Usage**

```
multiscale.localPrune(
  x,
  G = bandwidths.default(length(x)),
  max.unbalance = 4,
  threshold = c("critical.value", "custom")[1],
  alpha = 0.1,
  threshold.function = NULL,
  criterion = c("eta", "epsilon")[1],
  eta = 0.4,
  epsilon = 0.2,
  rule = c("pval", "jump")[1],
  penalty = c("log", "polynomial")[1],
  pen.exp = 1.01,
  do.confint = FALSE,
  level = 0.05,
  N_reps = 1000,
  ...
)
```

**Arguments**

x	input data (a numeric vector or an object of classes <code>ts</code> and <code>timeSeries</code> )
G	a vector of bandwidths, given as either integers less than $\text{length}(x)/2$ , or numbers between 0 and 0.5 describing the moving sum bandwidths relative to $\text{length}(x)$ . Asymmetric bandwidths obtained as the Cartesian product of the set G with itself are used for change-point analysis
max.unbalance	a numeric value for the maximal ratio between maximal and minimal bandwidths to be used for candidate generation, $1 \leq \text{max.unbalance} \leq \text{Inf}$
threshold	string indicating which threshold should be used to determine significance. By default, it is chosen from the asymptotic distribution at the significance level $\alpha$ . Alternatively, it is possible to parse a user-defined function with <code>threshold.function</code>
alpha	a numeric value for the significance level with $0 \leq \alpha \leq 1$ . Use iff <code>threshold = "critical.value"</code>
threshold.function	function object of form <code>function(G_l, G_r, length(x), alpha)</code> , to compute a threshold of significance for different bandwidths ( $G_l, G_r$ ); use iff <code>threshold = "custom"</code>
criterion	how to determine whether an exceeding point is a change-point; to be parsed to <a href="#">mosum</a>
eta, epsilon	see <a href="#">mosum</a>
rule	string for the choice of sorting criterion for change-point candidates in merging step. Possible values are: <ul style="list-style-type: none"> <li>• "pval" smallest p-value</li> <li>• "jump" largest (rescaled) jump size</li> </ul>
penalty	string specifying the type of penalty term to be used in Schwarz criterion; possible values are: <ul style="list-style-type: none"> <li>• "log" use <math>\text{penalty} = \log(\text{length}(x))^{\text{pen.exp}}</math></li> <li>• "polynomial" use <math>\text{penalty} = \text{length}(x)^{\text{pen.exp}}</math></li> </ul>
pen.exp	exponent for the penalty term (see <code>penalty</code> );
do.confint	flag indicating whether confidence intervals for change-points should be computed
level	use iff <code>do.confint = TRUE</code> ; a numeric value ( $0 \leq \text{level} \leq 1$ ) with which $100(1-\text{level})\%$ confidence interval is generated
N_reps	use iff <code>do.confint = TRUE</code> ; number of bootstrap replicates to be generated
...	further arguments to be parsed to <a href="#">mosum</a> calls

**Details**

See Algorithm 2 in the first referenced paper for a comprehensive description of the procedure and further details.

**Value**

S3 object of class `multiscale.cpts`, which contains the following fields:

<code>x</code>	input data
<code>cpts</code>	estimated change-points
<code>cpts.info</code>	data frame containing information about estimated change-points
<code>sc</code>	Schwarz criterion values of the estimated change-point set
<code>pooled.cpts</code>	set of change-point candidates that have been considered by the algorithm
<code>G</code>	input parameter
<code>threshold, alpha, threshold.function</code>	input parameters
<code>criterion, eta, epsilon</code>	input parameters
<code>rule, penalty, pen.exp</code>	input parameters
<code>do.confint</code>	input parameter
<code>ci</code>	object of class <code>cpts.ci</code> containing confidence intervals for change-points iff <code>do.confint = TRUE</code>

**References**

- A. Meier, C. Kirch and H. Cho (2021) mosum: A Package for Moving Sums in Change-point Analysis. *Journal of Statistical Software*, Volume 97, Number 8, pp. 1-42. <doi:10.18637/jss.v097.i08>.
- H. Cho and C. Kirch (2020) Two-stage data segmentation permitting multiscale change points, heavy tails and dependence. *arXiv preprint arXiv:1910.12486*.

**Examples**

```
x <- testData(model = "mix", seed = 123)$x
mlp <- multiscale.localPrune(x, G = c(8, 15, 30, 70), do.confint = TRUE)
print(mlp)
summary(mlp)
par(mfcol=c(2, 1), mar = c(2, 4, 2, 2))
plot(mlp, display = "data", shaded = "none")
plot(mlp, display = "significance", shaded = "CI", CI = "unif")
```

---

persp3D.multiscaleMosum

*3D Visualisation of multiscale MOSUM statistics*

---

**Description**

3D Visualisation of multiscale MOSUM statistics.

**Usage**

```

persp3D.multiscaleMosum(
  x,
  mosum.args = list(),
  threshold = c("critical.value", "custom")[1],
  alpha = 0.1,
  threshold.function = NULL,
  pal.name = "YlOrRd",
  expand = 0.2,
  theta = 120,
  phi = 20,
  xlab = "G",
  ylab = "time",
  zlab = "MOSUM",
  ticktype = "detailed",
  NAcol = "#800000FF",
  ...
)

```

**Arguments**

<code>x</code>	a numeric input data vector
<code>mosum.args</code>	a named list containing further arguments to be parsed to the respective <code>mosum</code> function calls, see <a href="#">mosum</a> ; the bandwidths are chosen by the function and should not be given as an argument in <code>mosum.args</code>
<code>threshold</code>	string indicating which threshold should be used for normalisation of MOSUM statistics computed with different bandwidths. By default, it is chosen from the asymptotic distribution at the given significance level $\alpha$ . Alternatively it is possible to parse a user-defined numerical value with <code>threshold.custom</code> ; see also <a href="#">Details</a> .
<code>alpha</code>	a numeric value for the significance level with $0 \leq \alpha \leq 1$ ; use iff <code>threshold = "critical.value"</code>
<code>threshold.function</code>	function object of form <code>function(G)</code> , to compute a threshold of significance for different bandwidths $G$ ; use iff <code>threshold='custom'</code>
<code>pal.name</code>	a string containing the name of the ColorBrewer palette to be used; sequential palettes are recommended. See <code>RColorBrewer::brewer.pal.info</code> for details
<code>expand</code>	expansion factor applied to the z coordinates
<code>theta</code>	azimuthal angle defining the viewing direction
<code>phi</code>	colatitude angle defining the viewing direction
<code>xlab, ylab, zlab, ticktype</code>	graphical parameters
<code>NAcol</code>	coloring parameter
<code>...</code>	further arguments to be passed to function call of <a href="#">persp3D</a>

## Details

The visualisation is based on [persp3D](#). MOSUM statistics computed with different bandwidths are rescaled for making them visually comparable. Rescaling is done either by dividing by their respective critical value at the significance level alpha (iff `threshold = "critical.value"`) or by a custom value given by `threshold.function` (iff `threshold = "custom"`). By default, `clim` argument of [persp3D](#) is given so that the three lightest (for sequential palettes) hues indicate insignificance of the corresponding MOSUM statistics, while darker hues indicate the presence of significant changes.

## Value

see [persp3D](#)

## Examples

```
## Not run:
# If you run the example be aware that this may take some time
print("example may take some time to run")

x <- testData(model = "blocks", seed = 1234)$x
persp3D.multiscaleMosum(x, mosum.args = list(boundary.extension = FALSE))

## End(Not run)
```

---

plot.mosum.cpts

*Plotting the output from MOSUM procedure*

---

## Description

Plotting method for S3 objects of class `mosum.cpts`

## Usage

```
## S3 method for class 'mosum.cpts'
plot(
  x,
  display = c("data", "mosum")[1],
  cpts.col = "red",
  critical.value.col = "blue",
  xlab = "Time",
  ...
)
```

**Arguments**

x	a mosum.cpts object
display	which to be plotted against the change-point estimators; possible values are <ul style="list-style-type: none"> <li>• "data" input time series is plotted along with the estimated piecewise constant signal</li> <li>• "mosum" scaled MOSUM detector values are plotted</li> </ul>
cpts.col	a specification for the color of the vertical lines at the change-point estimators, see <a href="#">par</a>
critical.value.col	a specification for the color of the horizontal line indicating the critical value, see <a href="#">par</a> ; use iff display = "mosum"
xlab	graphical parameter
...	additional graphical arguments, see <a href="#">plot</a> and <a href="#">abline</a>

**Details**

The location of each change-point estimator is plotted as a vertical line against the input time series and the estimated piecewise constant signal (display = "data") or MOSUM detector values (display = "mosum").

**Examples**

```
x <- testData(lengths = rep(100, 3), means = c(0, 5, -2), sds = rep(1, 3), seed = 1234)$x
m <- mosum(x, G = 40)
par(mfrow = c(2, 1), mar = c(2.5, 2.5, 2.5, .5))
plot(m, display = "data")
plot(m, display = "mosum")
```

---

plot.multiscale.cpts *Plotting the output from multiscale MOSUM procedure*

---

**Description**

Plotting method for S3 objects of class "multiscale.cpts".

**Usage**

```
## S3 method for class 'multiscale.cpts'
plot(
  x,
  display = c("data", "significance")[1],
  shaded = c("CI", "bandwidth", "none")[1],
  level = 0.05,
  N_reps = 1000,
  CI = c("pw", "unif")[1],
  xlab = "Time",
  ...
)
```

**Arguments**

x	a multiscale.cpts object
display	which to be plotted against the estimated change-point locations; possible values are <ul style="list-style-type: none"> <li>• "data" input time series is plotted along with the estimated piecewise constant signal</li> <li>• "significance" one minus the p-values associated with the detection of change-point estimators are represented as the height of vertical lines indicating their locations</li> </ul>
shaded	string indicating which to display as shaded areas surrounding the estimated change-point locations. Possible values are <ul style="list-style-type: none"> <li>• "bandwidth" respective detection intervals are plotted</li> <li>• "CI" bootstrap confidence intervals are plotted</li> <li>• "none" none is plotted</li> </ul>
level, N_reps	argument to be parsed to <code>confint.multiscale.cpts</code> ; use iff shaded = "CI".
CI	string indicating whether pointwise (CI = "pw") or uniform (CI = "unif") confidence intervals are to be plotted; use iff shaded = "CI"
xlab	graphical parameter
...	not in use

**Details**

The locations of change-point estimators are plotted against the input time series and the estimated piecewise constant signal (`display = "data"`), or the significance of each estimator is represented by the corresponding  $1-p$  value derived from the asymptotic distribution of MOSUM test statistic (`display = "significance"`). It also produces the rectangles representing the detection intervals (if `shaded = "bandwidth"`) or bootstrap confidence intervals of the corresponding change-points (if `shaded = "CI"`) around their locations.

**Examples**

```
x <- testData(model = "blocks", seed = 1234)$x
mlp <- multiscale.localPrune(x)
par(mfrow = c(2, 1))
plot(mlp, display = "data", shaded = "bandwidth")
plot(mlp, display = "significance", shaded = "CI")
```

---

print.mosum.cpts

*Change-points estimated by MOSUM procedure*


---

**Description**

Print method for objects of class `mosum.cpts`



### Usage

```
## S3 method for class 'mosum.cpts'  
print(x, ...)
```

### Arguments

x	a mosum.cpts object
...	not in use

### Examples

```
x <- testData(lengths = rep(100, 3), means = c(0, 5, -2), sds = rep(1, 3), seed = 1234)$x  
m <- mosum(x, G = 40)  
print(m)
```

---

`print.multiscale.cpts` *Change-points estimated by multiscale MOSUM procedure*

---

### Description

Print method for objects of class `multiscale.cpts`

### Usage

```
## S3 method for class 'multiscale.cpts'  
print(x, ...)
```

### Arguments

x	a multiscale.cpts object
...	not in use

### Examples

```
x <- testData(model = "mix", seed = 12345)$x  
mlp <- multiscale.localPrune(x)  
print(mlp)
```

---

```
summary.mosum.cpts      Summary of change-points estimated by MOSUM procedure
```

---

**Description**

Summary method for objects of class mosum.cpts

**Usage**

```
## S3 method for class 'mosum.cpts'
summary(object, ...)
```

**Arguments**

```
object      a mosum.cpts object
...         not in use
```

**Details**

Provide information about each estimated change-point, including the bandwidths used for its estimation, associated p-value and (scaled) jump size; if object\$do.confint=TRUE, end points of the pointwise and uniform confidence intervals are also provided.

**Examples**

```
x <- testData(lengths = rep(100, 3), means = c(0, 5, -2), sds = rep(1, 3), seed = 1234)$x
m <- mosum(x, G = 40, do.confint = TRUE)
summary(m)
```

---

```
summary.multiscale.cpts
      Summary of change-points estimated by multiscale MOSUM procedure
```

---

**Description**

Summary method for objects of class multiscale.cpts

**Usage**

```
## S3 method for class 'multiscale.cpts'
summary(object, ...)
```

**Arguments**

```
object      a multiscale.cpts object
...         not in use
```

## Details

Provide information about each estimated change-point, including the bandwidths used for its detection, associated p-value and (scaled) jump size; if `object$do.confint=TRUE`, end points of the pointwise and uniform confidence intervals are also provided.

## Examples

```
x <- testData(model = "mix", seed = 12345)$x
mlp <- multiscale.localPrune(x, do.confint = TRUE)
summary(mlp)
```

---

testData	<i>Test data with piecewise constant mean</i>
----------	---

---

## Description

Generate piecewise stationary time series with independent innovations and change-points in the mean.

## Usage

```
testData(
  model = c("custom", "blocks", "fms", "mix", "stairs10", "teeth10")[1],
  lengths = NULL,
  means = NULL,
  sds = NULL,
  rand.gen = rnorm,
  seed = NULL,
  ...
)
```

## Arguments

model	a string indicating from which model a realisation is to be generated; possible values are "custom" (for user-specified model using lengths, means and sds), and "blocks", "fms", "mix", "stairs10", "teeth10" (for the referenced test signals)
lengths	use iff model = "custom"; an integer vector for the lengths of the piecewise stationary segments
means	use iff model = "custom"; a numeric vector for the means of the piecewise stationary segments
sds	use iff model = "custom"; a numeric vector for the deviation scaling of the piecewise stationary segments. The values are multiplied to the outcome of rand.gen, coinciding with the standard deviation in the case of standard normal innovations (rand.gen = rnorm)
rand.gen	optional; a function to generate the noise/innovations

seed            optional; if a seed value is provided (!is.null(seed)), then set.seed(seed) is called beforehand)

...            further arguments to be parsed to rand.gen

### Details

See Appendix B in the reference for details about the test signals.

### Value

a list containing the following entries:

- x a numeric vector containing a realisation of the piecewise time series model, given as signal + noise
- mu mean vector of piecewise stationary time series model
- sigma scaling vector of piecewise stationary time series model
- cpts a vector of change-points in the piecewise stationary time series model

### References

P. Fryzlewicz (2014) Wild Binary Segmentation for Multiple Change-Point Detection. *The Annals of Statistics*, Volume 42, Number 6, pp. 2243-2281.

### Examples

```
# visualise estimated changepoints by solid vertical lines
# and true changepoints by broken vertical lines
td <- testData(lengths = c(50, 50, 200, 300, 300), means = c(0, 1, 2, 3, 2.3),
sds = rep(1, 5), seed = 123)
mbu <- multiscale.bottomUp(td$x)
plot(mbu, display = "data")
abline(v = td$cpts, col = 2, lwd = 2, lty = 2)

# visualise estimated piecewise constant signal by solid line
# and true signal by broken line
td <- testData("blocks", seed = 123)
mlp <- multiscale.localPrune(td$x)
plot(mlp, display = "data")
lines(td$mu, col = 2, lwd = 2, lty = 2)
```

# Index

`abline`, [15](#)

`bandwidths.default`, [2](#)

`confint.mosum.cpts`, [3](#)

`confint.multiscale.cpts`, [4](#), [16](#)

`mosum`, [5](#), [9](#), [11](#), [13](#)

`mosum.criticalValue`, [7](#)

`multiscale.bottomUp`, [8](#)

`multiscale.localPrune`, [10](#)

`par`, [15](#)

`persp3D`, [13](#), [14](#)

`persp3D.multiscaleMosum`, [12](#)

`plot`, [15](#)

`plot.mosum.cpts`, [14](#)

`plot.multiscale.cpts`, [15](#)

`print.mosum.cpts`, [16](#)

`print.multiscale.cpts`, [17](#)

`summary.mosum.cpts`, [18](#)

`summary.multiscale.cpts`, [18](#)

`testData`, [19](#)